

Unit :- 01

16/08/2022

Data :- Raw facts and figures in the form of values are called data

Data structure :- It is organizing and arranging the data so that it becomes easily

OR

logical & mathematical model of a particular organisation of data is called data structure

⇒ Type of data structures

- Linear data structure
- Non-linear data structure
- Homogeneous data structure
- Non-homogeneous data structure
- Primitive data structure
- Non primitive data structure
- static data structure
- Dynamic data structure

→ Linear data structure :- It is a type of a data structure in which data items are arranged in linear sequence for ex:- array, stack, queue

→ Non linear data structure :- element are not in sequence for ex :- tree and graph

→ Homogeneous data structure :- elements are of same type ex :- array.

→ Non Homogeneous data structure :- elements may or may not be of same type ex :- structured

→ Primitive data structure :- It is provided by programming language as basic building blocks. ex :- int, float, double, char.

→ Non primitive data structure :- It is derived from primitive data structure ex :- stack, queue etc.

→ Static data structure :- Memory is allocated at compile time

→ Dynamic data structure :- Memory is allocated at run time.

Stack example

```
class stack
{
    int a[10], top;
public:
    stack();
    void push(int);
```

```
int pop();
int peek();
```

```
void atack :: atack()
{ top = -1; }
void atack :: push(int x)
{ top++;
  a[top] = x;
}
```

```
int atack :: pop();
{ int t;
  t = a[top];
  top--;
  return t;
}
```

```
int atack :: peek()
{ return a[top]; }
```

class stack

```
int a[10], top;
public: stack();
void push(int);
int pop();
void display();
int peek();
};
stack s; stack();
top = -1;
```

```
void stack :: push(int x)
{
  top++;
  if (top < 9)
  { top++;
    a[top] = x;
  }
  else {
    cout << "Space overflow";
  }
  int stack :: pop()
  if (top >= 0)
  { int t = a[top];
    top--;
    return t;
  }
  else { cout << "no element left to pop"; }
}
```

⇒ Making dynamic allocation for array

```
class stack
{ int *p;
  int size, top;
public:
  stack() {}
  stack() {
    cout << "Enter size of array"
    cin >> size;
    p = new int[size];
  }
}
```

```

void push(int);
int pop();
int peek();
void disp();
~ stack() { delete p; }

int stack::pop()
{
    if (top < 0)
        cout << "stack
        overflow";
    else { int t = a[top];
          top--;
          return t;
        }
}
stack::stack()
{ top = -1; }
void stack::push(int x)
{
    if (top < (size - 1))
        top++;
    a[top] = x;
}
else
    cout << "stack is full";
}

```

Converting Infix to Postfix
 Operator maintains same order. Parenthesis not needed and priority of operators is not needed.

Algorithm

1. scan every character in infix string till end of the string
2. following steps are performed depending on the type of character scan
 - (i) if character scanned is a space then skip that character
 - (ii) if it is digit or alphabet then add it to target string

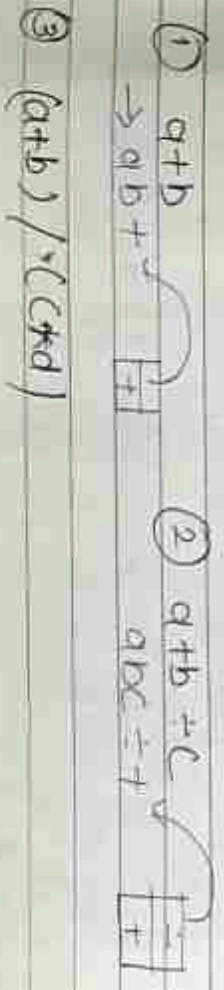
(iii) if it is opening parenthesis then add it to stack.

(iv) if it is an operator then compare the priority of topmost operator, topmost element from stack and the scanned character

3. following steps are occ. to precedence

- (i) if the priority of operator is higher or same as scanned character / operator then add the operator to the target string and push scanned character to stack
- (ii) if the operator is of low priority then scanned character then add it to stack
- (iii) if it is closing parenthesis then operator in the stack are retrieved then and add it to target string till it doesn't read opening parenthesis
- (iv) if scanner string exhaust then all operators in the stack are popped and add it to target string

Examples of Infix to Postfix

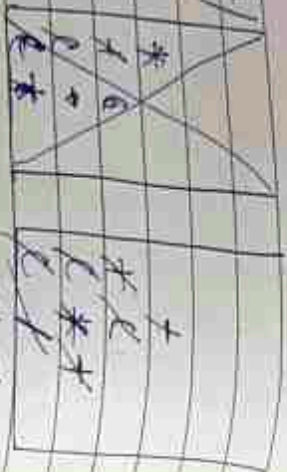


Soln $\rightarrow ab + cd + *$



① $((A+B)*C - (D-E)) / (E+F)$

Soln $\rightarrow ab + c + d * e - f + g$



Infix to postfix

Algorithm :-

1. Reverse the Infix string and about adding character to target string from last
2. Scan every character of source string following steps are followed depending upon the character scanned
 - (i) If the character scanned is space then skip
 - (ii) If it is digit or alphabet then add it target string
 - (iii) If it is closing parentheses then add to stack

v) If it is operator then compare the priority of topmost element from stack & scanned character, & acc. to the precedence perform following steps.

① If operator has higher precedence then add operator to target string and push scanned character to stack

② If operator has lower or same precedence then push scanned character to stack.

v) If it is an opening parenthesis then operator from stack are popped and added to target string till closing parentheses not reached.

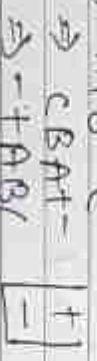
3. If source string exhausted then add all operators from stack to target string

Example

① $A+B$



② $A+B-C$



③ $A+B*C$



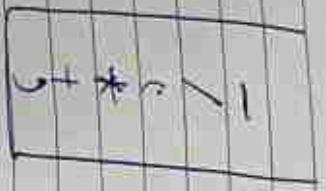
④ $(A+B) * (C-D)$



⑤ $A - B / (C * D + E)$

$\Rightarrow E D C * + B / A -$

$\Rightarrow - A / B + * C D E$



⇒ Evaluate the postfix

⇒ Algorithm

1. Scan the postfix expression char by char
2. If char scanned is an operator then push it to stack
3. If char scanned is space then skip it
4. If it is operator then pop the topmost elements from stack and operation is performed on operands

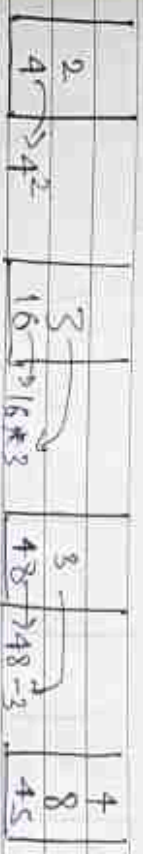
Example 8

① $((A + B) * C - (D - E)) / (F + G)$

Postfix: $AB + C * D E - F G + /$
 Let $A=4, B=6, C=2, D=8, E=2, F=1, G=1$



② $4 2 \wedge 3 * 3 - 8 4 / 1 1 + / +$



⇒ Reevaluation of postfix reverse string go 2nd element hoge upto pophle likhoge

① $((A + B) * C - (D - E)) / (F + G)$

Reverse string: $GF + ED - (BA + G) - /$

$GF + ED - (BA + G) - /$
 $GF + ABG - ED + + G$
 $GF + ABG - ED + FG$

A=4, B=6, C=2, D=8, E=2
 f=1, g=1

Prefix: ABC - DEFQ
 Infix: 462 - 220 + 11

1	1	1	1	1	1	1	1	1	1
2	2	2	2	2	2	2	2	2	2
4	4	4	4	4	4	4	4	4	4
6	6	6	6	6	6	6	6	6	6
8	8	8	8	8	8	8	8	8	8
10	10	10	10	10	10	10	10	10	10
12	12	12	12	12	12	12	12	12	12
14	14	14	14	14	14	14	14	14	14
16	16	16	16	16	16	16	16	16	16
18	18	18	18	18	18	18	18	18	18
20	20	20	20	20	20	20	20	20	20

14	7
2	7

② (8+2)* (6/2) + (10*5) convert into prefix and postfix and then evaluate

③ evaluate +- * ^ 4 2 3 3 // 8 9 + 11 in prefix form

soln 2 Postfix -

3 2 + 6 2 / * 10 5 * +

evaluate :-

2	6	3	5	10	15	65
3	5	15	15	15	15	65

)))))))
+	/	*	*	*	*	*
(((((((

=> 65

Prefix: 5 10 * 2 6 / 2 3 + * +

evaluation + * + 8 2 / 6 2 * 10 5

5	10	5	2	3	5	15	65
5	10	5	2	3	5	15	65

))))))))
*	*	*	*	*	*	*	*
((((((((

=> 65

soln 3 evaluating :-

1	8	2	16	48	45	46
1	4	2	3	3	3	1
1	2	2	1	1	1	1

QUEUE

class queue

{ int q[10];

int f, r;

public: queue ();

void add_element (int);

int del_element ();

};

queue q;

q[0] = 1; q[1] = 2; q[2] = 3; q[3] = 4; q[4] = 5; q[5] = 6; q[6] = 7; q[7] = 8; q[8] = 9; q[9] = 10;

```

for (int i=0; i<10; i++)
    q[i] = -1;
}
void queue :: add_element (int a)
{
    if (r < 10)
        if (r == -1)
            f = r = 0; q[r] = a;
        else r++;
        q[r] = a;
    }
    else
        cout << "queue is full";
}
int queue :: del_element ()
{
    if (f < 20)
        int t = q[f]
        q[f] = -1
        if (f == r)
            f = r = -1;
        else
            f++;
    }
    return t;
}
else { cout << "queue is empty";
return -1;
}
}

```

Dynamic allocation of array

```

class queue
{
    int *q, size;
    public:
        queue ()
        void add_element (int);
        int del_element ();
        ~queue ()
        { delete q; }
};
queue :: queue (int X = 10)
{
    size = X;
    q = new int [size]
    r = f = -1;
    for (int i=0; i<size; i++)
        q[i] = -1;
}
void queue :: add_element (int a)
{
    if (r < size)
        q[r] = a;
        r++;
    else
        cout << "queue is full";
}
}

```

```
int queue :: del_element ()
{
    if (f >= 0)
```

```
        int t = q[f];
        q[f] = -1;
        if (f == r)
            f = r = -1;
        else
            f++;
    }
    return t;
}
else
    cout << "queue empty";
return -1;
```

Circular Queue

```
class queue
{
    int q[10], f, r;
public:
    queue () { f = r = -1; }
    void add_ele(int);
    int del_ele ();
    void disp ();
};
```

```
void queue :: add_element (x)
{
    if ((r == max-1 && f == 0) || f == r+1)
```

```
        cout << "queue is full";
        return;
    }
    if (f == -1 && r == -1)
        f = r = 0;
    else if (r < q)
        r = r+1;
    else if (r == q && f == 0)
        r = 0;
    q[r] = x;
}

int queue :: del_ele ()
{
    int t = -1;
    if (f == -1)
        cout << "queue is empty";
        return t;
    t = q[f];
    q[f] = -1;
    if (f == r)
        f = r = -1;
    else if (f == 0)
        f = 0;
    else
        f++;
    return t;
}
```


D Queue

```
class dq {
public:
    int q[10], f, r;
    dq() {
        f = r = -1;
    }
    void add_ele(int);
    int del_ele();
};

dq::dq() {
    f = r = -1;
}

void dq::add_ele(int x) {
    if (f == 0) {
        cout << "item can't be added from front";
    }
    if (f == -1) {
        f = r = 0;
    }
    else {
        f--;
        q[f] = x;
    }
}

int dq::del_ele() {
    if (f == -1) {
        cout << "queue is empty";
        return -1;
    }
    int v = q[r];
    q[r] = -1;
}
```

```

if (f == r)
    f = r = -1;
else
    r--;
return v;
}

```

Linked List

```

struct node
{
    int d;
    node *next;
};
class linked_list
{
    node *start;
public:
    linked_list() { start = NULL; }
    void add_ele(int);
    void del_ele(); void display();
};
void linked_list::add_ele(int dd)
{
    node *t = new node;
    t->d = dd;
    t->next = NULL;
    if (start == NULL)
        start = t;
    else { node *temp;
           temp = start;

```

```

while (temp->next != NULL)
{
    temp = temp->next;
    temp->next = t;
}

```

```

}
void linked_list::del_ele(int dd)
{
    if (start == NULL)
    {
        cout << "List is empty";
        return;
    }
    node *temp, *old;
    temp = start;
    if (start->d == dd)
    {
        start = start->next;
        f = 1;
        delete temp;
    }
    else {
        while (temp != NULL)
        {
            if (temp->d == dd)
            {
                old->next = temp->next;
                delete temp;
                f = 1;
            }
            else {
                old = temp;
                temp = temp->next;
            }
        }
    }
    if (f == 0)
    {
        cout << "element not found";
    }
}

```

```

void linked_list::display()
{
    node * temp;
    start = temp;
    if (start == NULL)
        cout << "list is empty";
    else
        while (temp != NULL)
            cout << temp->d;
            temp = temp->next;
}

```

```

void linked_list::count()
{
    int c = 0;
    node * temp = start;
    while (temp != NULL)
    {
        c++;
        temp = temp->next;
    }
}

```

Adding node at beginning

```

struct node
{
    int d;
    node * link;
};

class linked_list
{
    node * start;
public:
    linked_list() { start = NULL; }
    void add_begin(int);
    void insert(int, int);
}

```

```

void linked_list::add_begin(int x)
{
    node * temp = new node;
    temp->d = x;
    temp->link = start;
    start = temp;
}

```

```

void linked_list::insert(int l, int x)
{
    int c = count();
    if (l <= (c+1) && l > 0)
    {
        if (l == 1)
            add_begin(x);
        else if (l == (c+1))
            add_end(x);
        else
        {
            node * temp = start;
            node * t = new node;
            t->d = x;
            for (int i = 1; i < (l-1); i++)
            {
                temp = temp->link;
            }
            t->link = temp->link;
            temp->link = t;
        }
    }
}

```

Stack using LL

```
struct node
{
    int d;
    node *link;
}

class stack
{
    node *tos;
public:
    stack() { tos = NULL; }
    void push(int);
    int pop();
};
```

```
void stack::push(int x)
{
    node *temp = new node;
    temp->d = x;
    temp->link = tos;
    tos = temp;
}
```

```
int stack::pop()
{
    if (tos == NULL)
        cout << "Stack is empty";
    else
    {
        node *temp = tos;
        int dd = temp->d;
        tos = temp->link;
        delete temp;
        return dd;
    }
}
```

Queue using LL

```
struct node
{
    int d;
    node *link;
}

class queue
{
    node *f, *r;
public:
    queue() { f = r = NULL; }
    void add_node(int);
    int del_node();
};
```

```
void queue::add_node(int x)
{
    node *temp = new node;
    temp->d = x;
    temp->link = NULL;
    if (r == NULL)
        r = f = temp;
    else
        r->link = temp;
    r = temp;
}
```

```
int queue::del_node()
{
    if (f == NULL)
        cout << "Queue is empty";
    else
    {
        node *temp = f;
        f = f->link;
        delete temp;
        return temp->d;
    }
}
```

8

```
f = f -> link;
int t = temp -> d;
delete temp;
if (f == NULL)
    u = NULL;
return t;
}
```

Input restricted DQueue

```
struct node
{
    int d;
    node * link;
}
```

```
class Dqueue
{
    node * f, * r;
public:
    Dqueue() { f = r = NULL; }
    void add-node(int);
    int del-node();
};

int del-node()
{
    if (f == NULL)
    {
        cout << "Queue is empty";
        return -1;
    }
    int t;
    else if (f == r)
```

```
} t = r -> d;
delete r;
r = f = NULL;
return t;
}
```

```
while (temp -> link -> link != NULL)
{
    temp = temp -> link;
    u = temp;
    temp = temp -> link;
    delete temp;
    return t;
}
```

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Doubly linked list

```
struct node
{
    int d;
    node * prev, * next;
}
```

```
class dlinkedlist
{
    node * start;
public:
    dlinkedlist()
    {
        start = NULL;
    }
    void append-node(int);
    int delete(int);
};
```

```

# void dlinkedlist :: append_node (int x)
{
    node *t, *temp;
    t = new node;
    t->d = x;
    if (start == NULL)
    {
        start = t;
        start->prev = NULL;
    }
    else { temp = start;
        while (temp->next != NULL)
        {
            temp = temp->next;
        }
        temp->next = t;
        t->prev = temp;
    }
}

```

```

void linkedlist :: delete (int x)
{
    if (start == NULL)
    {
        cout << "list is empty";
        return -1;
    }
    else { node *temp, *old, temp = start;
        int t, f = 0;
        if (start->d == x)
        {
            start = NULL; f = 1;
        }
        else {
            start = start->next;
            start->prev = NULL;
        }
    }
}

```

```

else {
    while (temp->next != NULL)
    {
        old = temp;
        temp = temp->next;
        if (temp->d == x)
        {
            f = 1;
            if (temp->next == NULL)
            {
                temp->prev->next = NULL;
            }
            else {
                old->next = temp->next;
                temp->next->prev = old;
            }
        }
    }
}
if (f == 1) { t = temp->d;
    delete temp;
    return t;
}
else { cout << "node not found";
    return -1;
}
}
void dlinkedlist :: add_node_begin (int x)
{
    node *temp = new node;
    temp->d = x;
    if (start == NULL)
    {
        start = temp;
        start->next = start->prev = NULL;
    }
}

```

```

else { temp->next = start;
      start->prev = temp;
      start = temp;
      start->prev = NULL;
    }
}

```

```

void dlinklist :: insert (int l, int x)
{
  int c = count();
  if (l > 0 & l < (c+2))
  {
    if (l == 1)
      add_node_beg (x);
    else if (l == (c+1))
      append (x);
    else { node *temp, *t;
          t = new node;
          t->d = x;
          temp = start;
          for (int i=1; i < (l-1); i++)
            temp = temp->next;
          t->next = temp->next;
          t->prev = temp;
          temp->next->prev = t;
          temp->next = t;
        }
    else { cout << "Invalid location"; }
  }
}

```

Searching

Linear Search

```

class array
{
  int a[5];
public:
  void get_element(); void display();
  void search_element();
} array;

void array::get_element()
{
  int n;
  for (int i=0; i < 5; i++)
  {
    cout << "Enter the element at " << i << "index";
    cin >> a[i];
  }
}

void array::display()
{
  for (int i=0; i < 5; i++)
  {
    cout << "element at a" << i << " is " << a[i];
  }
}

void array::search()
{
  int f=0, b;
  cout << "Enter value that you want to search";
  cin >> b;
}

```

```

for (i=0; i<5; i++)
{
    if (b == a[i])
    {
        cout << "element found";
        f = 1;
    }
}
if (f == 0) { cout << "element not found"; }
}

```

Binary search

```

class array
{
    int a[5], l;
    public:
    void get_element();
    void display();
    void search();
}

```

```

void array::get_element()
{

```

```

    for (i=0; i<5; i++)
    {
        cout << "Enter element at " << i << " index";
        cin >> a[i];
    }
}

```

```

void array::display()
{
    for (i=0; i<5; i++)
    {
        cout << "element at a" << i << " is " << a[i];
    }
}

```

```

void array::search()
{
    int l=0, u=4, m, f=0;

```

```

    for (m =  $\frac{l+u}{2}$ ; l <= u; m =  $\frac{l+u}{2}$ )

```

```

    {
        if (a[m] == x)
        {
            cout << "element found";
            f = 1;
            break;
        }

```

```

        else if (a[m] > x)
            u = m - 1;

```

```

        else
            l = m + 1;
    }

```

```

    if (f == 0)
    {
        cout << "element not found";
    }
}

```

Sorting

Selection sort

```

void sort()

```

```

{
    int i, j;
    for (i=0; i<n; i++)
    {
        for (j=i+1; j<n; j++)
        {
            if (a[i] > a[j])
            {
                int c;
                c = a[i];
                a[i] = a[j];
                a[j] = c;
            }
        }
    }
}

```


Bubble sort

```
void Bsort()
{
    int temp = 0;
    for (int i = 0; i < size - 1; i++)
    {
        for (int j = 0; j < size - i - 1; j++)
        {
            if (a[j] > a[j+1])
            {
                temp = a[j];
                a[j] = a[j+1];
                a[j+1] = temp;
            }
        }
    }
}
```

Quick sort :- It's a recursive algorithm
Algorithm :-

→ In first iteration

```
void quicksort (int low, int high)
{
    if (low < high)
    {
        partition (low, high);
        quicksort (low, j-1);
        quicksort (j+1, high);
    }
}
```

```
void partition (int lb, int ub)
```

```
{
    int pivot = a[lb];
    int down = lb+1;
    int up = ub;
    while (down <= up)
    {
        while (a[down] <= pivot)
            down++;
        while (a[up] > pivot)
            up--;
        if (up > down)
        {
            int temp = a[up];
            a[up] = a[down];
            a[down] = temp;
        }
    }
    a[lb] = a[up];
    a[up] = pivot;
    j = up;
}
```

Merge Sort

A	4	5	6	10	14		
B	2	3	8	12	13	16	20

int l = j = k = 0;

```

m=5, n=7;
int a[5], b[7], c[12];

```

```

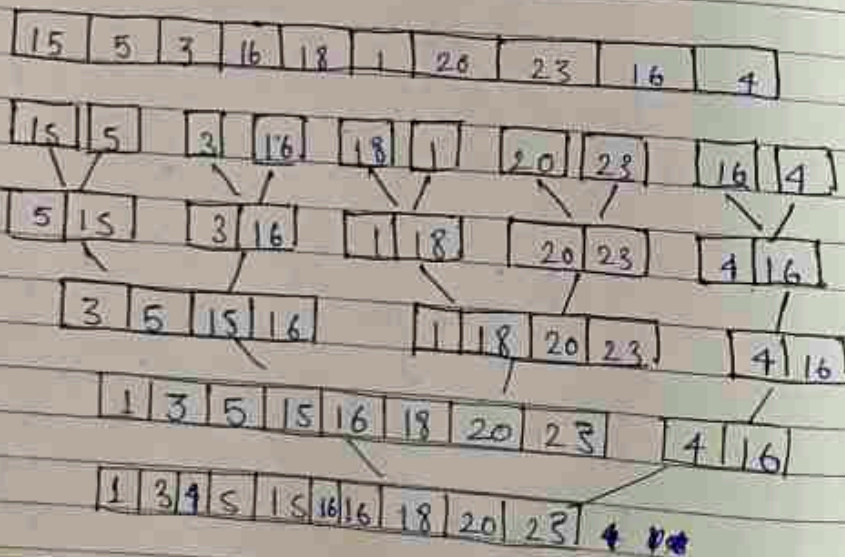
while (i < m && j < n)
{
    if (a[i] <= b[j])
        c[k++] = a[i++];
    else
        c[k++] = b[j++];
}

```

```

while (i < m)
{
    c[k++] = a[i++];
}
while (j < n)
    c[k++] = b[j++];

```



```

void mergesort()
{

```

```

    int size = 1, i, j;
    int lb1, lb2, ub1, ub2, temp[10];
    while (size <= n)

```

```

    {
        lb1 = 0;
        int x = 0;
        while (lb1 + size <= n - 1)
        {
            lb2 = lb1 + size;
            ub1 = lb2 - 1;

```

```

            if (lb2 + size - 1 > n - 1)
                ub2 = n - 1;

```

```

            else
                ub2 = lb2 + size - 1;

```

```

            i = lb1;
            j = lb2;

```

```

            while (i <= ub1 && j <= ub2)
            {

```

```

                if (arr[i] <= arr[j])
                    temp[x++] = arr[i++];
                else
                    temp[x++] = arr[j++];
            }

```

```

            while (i <= ub1)
                temp[x++] = arr[i++];
            lb1 = ub1 + 1; // increment condition

```

```
l = lb1;
```

```
while (k <= n-1)  
    temp[k++] = arr[i++]; // for single  
                           element
```

```
for (x=0; x <= n-1; x++)  
    arr[x] = temp[x]; // for copying
```

```
size = size * 2;
```

Insertion Sort

11/10/2022

```
void array :: isort ()
```

```
{  
    int i, j, k, temp;
```

```
    for (i=0; i < size; i++)
```

```
        for (j=0; j < i; j++)
```

```
            if (arr[j] > arr[i])
```

```
                temp = arr[i];
```

```
for (k=i; k > j; k--)
```

```
    arr[k] = arr[k-1];
```

```
arr[j] = temp;
```

Radix Sort

The Radix sort algorithm works on by ordering each digit from least significant to most significant. In base 10, radix sort would sort by the digits in the one's place, then the ten's place and so on. To sort the value in each digit place, Radix sort employees counting sort as a subroutine.

```
void Radix-sort ()
```

Tree

⇒ It is a non linear data structure

⇒ collection of nodes organized in hierarchical structure.

⇒ Node :- Each element of a tree is node.

⇒ Root :- Element that represent the base node

of the tree

⇒ Leaf :- The node who does not have any child

⇒ Degree of node :- No. of node connected to a node

⇒ Level :- root node \Rightarrow 0 level
level of other nodes will be one more than root node

⇒ Depth or height of tree :- maximum level of any leaf node in the tree is called any depth or height.

⇒ Binary tree :- A finite set of element that are either empty / partitioned into three (s) disjoint subsets. The first subset contains a single element called the root of the tree. The other two subsets are called left and right subsets of original tree

• A binary tree is called strictly binary

Just if every non-leaf node is a binary tree has non-empty left and right subtree

- A strictly binary tree all of whose leaf nodes are at same level is called complete binary tree

Sequence on the

Pre order traversal: visit the root node then traverse the left subtree then right subtree

General form: $P \rightarrow LR$

- ① Parent node
- ② Left subtree
- ③ Right subtree



Pre order traversal \Rightarrow A B D G C H I F

Pre order traversal

Left subtree

① In order traversal \Rightarrow L R P \rightarrow Left subtree then

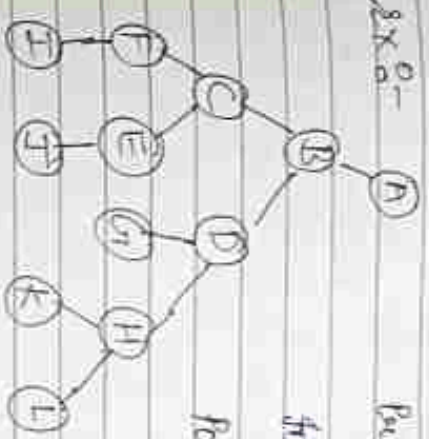
traverse \Rightarrow D G B A H E C F

② Post order traversal \Rightarrow L R P \Rightarrow G H D B H I F E C A

In-order: Pre: A B C F I E J D G H K L

In: F I C E J B G D K H L A

Post: J F E J C G D K H L A



& In-order representation: If node is at nth position then left will be at (n-1) and right will be at (n+1)